

Code: 17T00106A

Pharm.D I Year Advanced Supplementary Examinations February/March 2023

REMEDIAL MATHEMATICS

(For 2017, 2018, 2019, 2020 & 2021 admitted batches only)

Time: 3 hours

Max. Marks: 70

PART – A
(Compulsory Question)

1 Answer the following: (10 X 02 = 20 Marks)

- (a) Find the determinant of a matrix $A = \begin{bmatrix} 2 & 3 & 1 \\ 6 & 5 & 2 \\ 1 & 4 & 7 \end{bmatrix}$ 2M
- (b) What is the use of Cramer's rule? 2M
- (c) Find the equation of the line passing through the point (1, 1) and perpendicular to the line passing through the points (3, 5) and (-6, -2). 2M
- (d) If $a = 18$, $b = 24$ and $c = 30$ then find $\sin A$, $\sin B$ and $\sin C$. 2M
- (e) Solve the following system of equations by Cramer's rule $x - y + 2z = 7$, $3x + 4y - 5z = -5$, $2x - y + 3z = 12$. 2M
- (f) Integrate $\int \sin^4 x \, dx$. 2M
- (g) Solve $\frac{dy}{dx} = xy - y$. 2M
- (h) Solve: 2M
$$\frac{dy}{dx} = \frac{x+y}{x}$$
- (i) Find the Laplace transform of the function $\cos 2t$. 2M
- (j) Find the Laplace Transform of $e^{-t} \sin t$. 2M

PART – B

(Answer all five units, 5 X 10 = 50 Marks)

- 2 (a) Find the determinant of the matrix A where 5M
$$A = \begin{bmatrix} 1 & 3 & 2 \\ -3 & -1 & -3 \\ 2 & 3 & 1 \end{bmatrix}$$
- (b) If $A = \begin{bmatrix} 3 & 1 & 2 \\ 1 & 0 & 1 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & -1 \\ 2 & 1 \\ 3 & 1 \end{bmatrix}$, find AB 5M
- OR**
- 3 (a) Evaluate $\lim_{x \rightarrow 2} \frac{\frac{1}{x} - \frac{1}{2}}{x - 2}$. 5M
- (b) If $\sin A = 3/5$, $\cos B = 9/41$ then find the value of $\sin(A-B)$ and $\sin(A+B)$. 5M

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4 (a) If $y = a \cos(\log x) + b \sin(\log x)$ show that $x^2 y_{n+2} + (2n+1)xy_{n+1} + (n^2+1)y_n = 0$. 5M

(b) Find the n^{th} derivative of $\cos x \cos 2x \cos 3x$. 5M

OR

5 (a) If $z = f(x+ct) + \phi(x-ct)$, prove that $\frac{\partial^2 z}{\partial t^2} = c^2 \frac{\partial^2 z}{\partial x^2}$. 5M

(b) State and Prove Euler's theorem on Homogeneous function. 5M

6 (a) Find the value of $\int \frac{dx}{x(x-1)}$ 5M

(b) Find the value of $\int \sin^2 x dx$. 5M

OR

7 (a) Solve $\frac{dy}{dx} = xy - y$. 5M

(b) Solve $y'' - 3y' + 2y = xe^{3x}$. 5M

8 (a) Solve $\frac{dy}{dx} = 3x^2(y+2)$. 5M

(b) Solve $\frac{dy}{dx} = \frac{2y}{x(y-1)}$. 5M

OR

9 (a) Define: (i) Differential equation (ii) Order of a differential equation (iii) Degree of a differential equation (iv) Linear differential equation with an example. 5M

(b) Solve the differential equation $\frac{dy}{dx} + 2xy = e^{-x^2}$ 5M

10 (a) $e^{3t} \cos 5t + t \sin t + \frac{\cos t}{t}$ Find $L[f(t)]$. 5M

(b) Find $L(5 \sin t + 2 \sin 3t)$ 5M

OR

11 (a) Find $L\{e^{-t} \sin 6t + t \cos 3t\}$. 5M

(b) Find $L[e^{-t} \sin^2 t]$ 5M

Pharm.D I Year Advanced Supplementary Examinations April 2022

REMEDIAL MATHEMATICS

(For 2017, 2018, 2019 & 2020 admitted batches only)

Time: 3 hours

Max. Marks: 70

PART – A
(Compulsory Question)

1 Answer the following: (10 X 02 = 20 Marks)

(a) Find the inverse of the matrix $\begin{bmatrix} 2 & 3 & 4 \\ 4 & 3 & 1 \\ 1 & 2 & 4 \end{bmatrix}$.

(b) If $\tan(\cot x) = \cot(\tan x)$, then $\sin 2x$.

(c) Suppose $H(t) = t^2 + 5t + 3$. Find the $\lim_{t \rightarrow 2} H(t)$.

(d) If $y = e^{ax} \cos bx$, prove that $y_2 + 2ay_1 + (a^2 + b^2)y = 0$.

(e) Evaluate $\int_0^{1/2} \cos^2 x \, dx$.

(f) Evaluate $\int_0^{\pi/6} \sin^3 3\theta \, d\theta$.

(g) Solve $(x+1)\frac{dy}{dx} + 1 = 2e^{-y}$.

(h) Solve $\frac{dy}{dx} = \cos(x+y+1)$.

(i) Find the Laplace transform of $\sin 2t \sin 3t$.

(j) Find the Laplace transform of $\cos^2 2t$.

PART – B

(Answer all five units, 5 X 10 = 50 Marks)

2 (a) Reduce the matrix $\begin{bmatrix} -19 & 7 \\ -42 & 16 \end{bmatrix}$ to the diagonal form.

(b) IF $A = \begin{bmatrix} 3 & -1 & 1 \\ -1 & 5 & -1 \\ 1 & -1 & 3 \end{bmatrix}$ Calculate A^4 .

OR

3 (a) Reduce the matrix $\begin{bmatrix} -1 & 1 & -2 \\ 1 & 2 & 1 \\ -1 & -1 & 0 \end{bmatrix}$ to the diagonal form.

(b) Find the inverse of $\begin{bmatrix} 1 & 1 & 3 \\ 1 & 3 & -3 \\ -2 & -4 & -4 \end{bmatrix}$.

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- 4 (a) Find the nth derivative of $e^x (2x+3)^3$.
(b) If $y = a \cos(\log x) + b \sin(\log x)$ show that $x^2 y_{n+2} + (2n+1)xy_{n+1} + (n^2+1)y_n = 0$.

OR

- 5 (a) Find the nth derivative of $\log(4x^2-1)$.
(b) If $y = \tan^{-1} x$ prove that $(1+x^2)y_{n+2} + 2(n+1)xy_{n+1} + n(n+1)y_n = 0$.

- 6 (a) Evaluate $\int_0^{\pi} \sin^5(x/2) dx$.
(b) Evaluate $\int_0^{\pi} \sin^6 x \cos^4 x dx$.

OR

- 7 (a) Evaluate $\int_0^{\pi} \frac{\sin^4 \theta}{(1+\cos \theta)^2} dx$
(b) Evaluate $\int_0^2 \frac{x^4}{\sqrt{4-x^2}} dx$.

- 8 (a) Solve $y'' + 4y' + 4y = 3 \sin x$.
(b) Solve $(D-2)^2 = 8(\sin 2x + x^2)$.

OR

- 9 (a) Solve $y'' - 2y' + y = xe^x \cos x$.
(b) Solve $y'' - y = x \sin 3x$.

- 10 (a) Find the Laplace transform of $e^{2t} \cos^2 2t$.
(b) Find the Laplace transform of $\sqrt{t}e^{3t}$.

OR

- 11 (a) Find the Laplace transform of $3\sqrt{t} + \frac{4}{\sqrt{t}}$.
(b) Find the Laplace transform of $\left(\sqrt{t} - \frac{1}{\sqrt{t}}\right)^3$.

REMEDIAL MATHEMATICS

(For 2017, 2018 & 2019 admitted batches only)

Time: 3 hours

Max. Marks: 70

PART – A
(Compulsory Question)

1 Answer the following: (10 X 02 = 20 Marks)

(a) Determine the rank of the matrix $\begin{bmatrix} 1 & 2 & 3 \\ 1 & 4 & 2 \\ 2 & 6 & 5 \end{bmatrix}$.

(b) If the sides of a triangle are 13, 14, 15, then find $\frac{\sin A}{\sin B}$.

(c) If $y = ae^{nx} + be^{-nx}$, then prove that $y'' = n^2 y$.

(d) If $z = f(x+ct) + \phi(x-ct)$, then prove that $\frac{\partial^2 z}{\partial t^2} = c^2 \frac{\partial^2 z}{\partial x^2}$.

(e) Evaluate the integral $\int_0^4 \frac{x^2}{1+x} dx$.

(f) Evaluate $\int_0^{16} \frac{x^{1/4}}{1+x^{1/2}} dx$.

(g) Find the order and degree of $\left[\frac{d^2 y}{dx^2} + \left(\frac{dy}{dx} \right)^3 \right]^{6/5} = 6y$.

(h) Solve the differential equation $\frac{dy}{dx} + y \tan x = \cos^3 x$.

(i) Find the equation of the circle for which the points (1, 2) and (4, 6) are the end points of a diameter.

(j) Define Laplace transform.

PART – B

(Answer all five units, 5 X 10 = 50 Marks)

2 (a) Find the matrix A such that $\begin{bmatrix} 2 & 1 \\ 3 & 2 \end{bmatrix} A \begin{bmatrix} -3 & 2 \\ 5 & -3 \end{bmatrix} = \begin{bmatrix} -2 & 4 \\ 3 & -1 \end{bmatrix}$.

(b) (i) If $a = (b-c) \sec \theta$, prove that $\tan \theta = \frac{2\sqrt{bc}}{b-c} \sin \frac{A}{2}$.

(ii) If $a = 4$, $b = 5$, $c = 7$, find $\cos \frac{B}{2}$.

OR3 (a) Investigate the values of λ and μ so that the equations $2x+3y+5z=9$, $7x+3y-2z=8$, $2x+3y+\lambda z=\mu$, have: (i) No solution. (ii) A unique solution. (iii) An infinite number of solutions.

(b) In a ΔABC show that $\frac{b^2 - c^2}{a^2} = \frac{\sin(B-C)}{\sin(B+C)}$.

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- 4 (a) Check the continuity of the function given by $f(x) = \begin{cases} 4-x^2 & \text{if } x \leq 0 \\ x-5 & \text{if } 0 < x \leq 1 \\ 4x^2-9 & \text{if } 1 < x < 2 \\ 3x+4 & \text{if } x \geq 2 \end{cases}$ at the points 0, 1 and 2.

(b) If $y = ae^{-bx} \cos(cx+d)$ then, prove that $y'' + 2by' + (b^2 + c^2)y = 0$.

OR

- 5 (a) Show that $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = 2u \log u$ where $\log u = \frac{(x^3 + y^3)}{(3x + 4y)}$.

(b) If $y = (\sin^{-1} x)^2$, show that $(1-x^2)y_{n+2} - (2n+1)xy_{n+1} - n^2y_n = 0$ hence find $(y_n)_0$ by using Leibnitz theorem.

- 6 (a) (i) Evaluate $\int_1^4 x\sqrt{x^2-1} dx$.

(ii) Evaluate $\int_0^4 |2-x| dx$.

- (b) Evaluate $\lim_{n \rightarrow \infty} \left[\left(1 + \frac{1}{n}\right) \left(1 + \frac{2}{n}\right) \dots \left(1 + \frac{n}{n}\right) \right]^{1/n}$ by using definite integral as the limit of a sum.

OR

- 7 (a) Evaluate $\int_0^1 x \tan^{-1} x dx$.

(b) Evaluate $\int_0^{\pi} \frac{x \sin x}{1 + \cos^2 x} dx$.

- 8 (a) Solve $\frac{dy}{dx} = \frac{x^2 + y^2}{2x^2}$.

(b) Solve $\frac{d^2y}{dx^2} + \frac{dy}{dx} + y = (1 - e^x)^2$.

OR

- 9 (a) Solve the differential equation $\sin^2 x \frac{dy}{dx} + y = \cot x$.

(b) Solve $y'' + 4y' + 4y = 3 \sin x + 4 \cos x$.

- 10 (a) Find the equation of the tangents to the circle $x^2 + y^2 + 2x - 2y - 3 = 0$ which are perpendicular to $3x - y + 4 = 0$.

(b) Find Laplace transform of $\sin 2t \sin 3t$.

OR

- 11 (a) Find the foot of perpendicular drawn from $(3, 0)$ upon the straight line $5x + 12y - 41 = 0$.

(b) Find Laplace transform of $e^{-3t} (2 \cos 5t - 3 \sin 5t)$.

Code: 17T00106A

Pharm.D I Year Regular & Supplementary Examinations December 2021

REMEDIAL MATHEMATICS

(For 2017, 2018, 2019 & 2020 admitted batches only)

Time: 3 hours

Max. Marks: 70

PART – A

(Compulsory Question)

1 Answer the following: (10 X 02 = 20 Marks)

(a) Find the inverse of the matrix $\begin{bmatrix} 2 & 3 & 4 \\ 4 & 3 & 1 \\ 1 & 2 & 4 \end{bmatrix}$.

(b) If $\tan(\cot x) = \cot(\tan x)$, then $\sin 2x$.

(c) Suppose $H(t) = t^2 + 5t + 1$. Find the limit $\lim_{t \rightarrow 2} H(t)$.

(d) If $y = e^{ax} \sin bx$, prove that $y_2 - 2ay_1 + (a^2 + b^2)y = 0$.

(e) Evaluate $\int_0^{\pi/2} \cos^9 x dx$.

(f) Evaluate $\int_0^{\pi/6} \sin^3 3\theta d\theta$.

(g) Solve $(x^2 - y^2)dx = 2xydy$.

(h) Solve $x^2ydx - (x^3 + y^3)dy = 0$.

(i) Find the Laplace transform of $\cos 2t \cos 3t$.

(j) Find the Laplace transform of $\sin^3 2t$.

PART – B

(Answer all five units, 5 X 10 = 50 Marks)

2 (a) Express each of the following matrices as the sum of a symmetric and a skew symmetric matrix:

$$\begin{bmatrix} 3 & -2 & 6 \\ 2 & 7 & -1 \\ 5 & 4 & 0 \end{bmatrix}$$

(b) Find the inverse of $\begin{bmatrix} 2 & 3 & 4 \\ 4 & 3 & 1 \\ 1 & 2 & 4 \end{bmatrix}$.

OR

3 (a) $A = \begin{bmatrix} 1 & 1 & 2 \\ 1 & 9 & 3 \\ 1 & 4 & 2 \end{bmatrix}$ $B = \begin{bmatrix} 1 & 2 & 0 \\ 2 & 3 & -1 \\ 1 & -1 & 3 \end{bmatrix}$ verify that $(AB)^{-1} = B^{-1}A^{-1}$.

(b) Prove that $A^3 - 4A^2 - 3A + 11I = 0$ where $A = \begin{bmatrix} 1 & 3 & 2 \\ 2 & 0 & -1 \\ 1 & 2 & 3 \end{bmatrix}$.

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- 4 (a) Find the n^{th} derivative of $\frac{x}{1+3x+2x^2}$.
- (b) If $y = e^{m \cos^{-1} x}$ prove that $(1-x^2)y_{n+2} - (2n+1)xy_{n+1} - (n^2+m^2)y_n = 0$.

OR

- 5 (a) Find the n^{th} derivative of $x^5 + \log_{10}(3x^2 + 5x - 2)$.
- (b) If $y = x^2 e^x$ prove that $y_n = \frac{1}{2}n(n-1)y_2 - n(n-2)y_1 + \frac{1}{2}(n-1)(n-2)y$.

- 6 (a) Evaluate $\int_0^{\pi/6} \cos^4 3\theta \sin^3 6\theta d\theta$ using reduction formula.

(b) Evaluate $\int_0^1 x^{3/2} (1-x)^{3/2} dx$.

OR

7 (a) Evaluate $\int_0^{\pi/2} \sin^8 x \cos^6 x dx$.

(b) Evaluate $\int_0^{\pi} x \sin^2 x \cos^4 x dx$.

8 (a) Solve $y'' - 4y' + 4y = 3 \cos x$.

(b) Solve $(D-4)^2 = 8(\cos 2x + x^2)$.

OR

9 (a) Solve $y'' - 2y' + 2y = x + e^x \cos x$.

(b) Solve $y'' - y = x \cos 3x$.

10 (a) Find the Laplace transform of $t \sin at$.

(b) Find the Laplace transform of $e^{-t} \sin^2 t$.

OR

11 (a) Find the Laplace transform of $\cos t \cos 2t \cos 3t$.

(b) Find the Laplace transform of $\sin^2(2t+1)$.

Code: 17T00106A

Pharm.D I Year Regular & Supplementary Examinations December 2020

REMEDIAL MATHEMATICS

(For 2017, 2018 & 2019 admitted batches only)

Time: 3 hours

Max. Marks: 70

PART – A
(Compulsory Question)

1 Answer the following: (10 X 02 = 20 Marks)

(a) Find the inverse of $\begin{bmatrix} 1 & 1 & 3 \\ 1 & 3 & -3 \\ -2 & -4 & -4 \end{bmatrix}$.

(b) If $\tan \frac{A}{2} = \frac{5}{6}$ and $\tan \frac{C}{2} = \frac{2}{5}$, determine the relation between a, b, c.

(c) Compute the limit $\lim_{x \rightarrow \frac{\pi}{2}} \frac{\cos x}{\left(x - \frac{\pi}{2}\right)}$.

(d) If $z = x^3 + y^3 - 3axy$ then show that $\frac{\partial^2 z}{\partial y \partial x} = \frac{\partial^2 z}{\partial x \partial y}$.

(e) Evaluate the integral $\int_0^{\pi/2} \frac{\sin^3 x}{\sin^3 x + \cos^3 x} dx$.

(f) Evaluate $\int_{-\pi/2}^{\pi/2} \sin |x| dx$.

(g) Find the general solution of $x + y \frac{dy}{dx} = 0$.

(h) Solve $\frac{d^2 x}{dt^2} + 6 \frac{dx}{dt} + 9x = 0$.

(i) Find the vertex and focus of $4y^2 + 12x - 20y + 67 = 0$.

(j) State first shifting property.

PART – B

(Answer all five units, 5 X 10 = 50 Marks)

2 (a) Prove that the matrix $A = \begin{bmatrix} \frac{1}{2}(1+i) & \frac{1}{2}(-1+i) \\ \frac{1}{2}(1+i) & \frac{1}{2}(1-i) \end{bmatrix}$ is unitary and find A^{-1} .

(b) In ΔABC , if $\frac{1}{a+c} + \frac{1}{b+c} = \frac{3}{a+b+c}$, show that $C = 60^\circ$.

OR

3 (a) Solve the following system of equations by matrix method $2x - y + 3z = 8$, $x - 2y - z = -4$, $3x + y - 4z = 0$.

(b) If the angles of ΔABC are in the A.P and $b : c = \sqrt{3} : \sqrt{2}$, then show that $A = 75^\circ$.

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Code: 17T00106A

- 4 (a) Verify whether the following function is differentiable at 1 and 3.

$$f(x) = \begin{cases} x & \text{if } x < 1 \\ 3 - x & \text{if } 1 \leq x \leq 3 \\ x^2 - 4x + 3 & \text{if } x > 3 \end{cases}$$

- (b) If $ax^2 + 2hxy + by^2 = 1$, then prove $\frac{d^2y}{dx^2} = \frac{h^2 - ab}{(hx + by)^3}$.

OR

- 5 (a) If $u = \sin^{-1} \frac{x + 2y + 3z}{x^2 + y^2 + z^2}$, find the value of $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} + z \frac{\partial u}{\partial z}$.

- (b) Find the n^{th} derivative of $e^x (2x + 3)^3$ by using Leibnitz theorem.

- 6 (a) Evaluate $\lim_{n \rightarrow \infty} \frac{2^k + 4^k + 6^k + \dots + (2n)^k}{n^{k+1}}$ by using definite integral as the limit of a sum.

- (b) Evaluate $\int_0^{\pi/4} \log(1 + \tan x) dx$.

OR

- 7 (a) Evaluate $\int_0^{\pi} \frac{x \sin^3 x}{1 + \cos^2 x} dx$.

- (b) Evaluate $\int_0^1 \frac{\log(1+x)}{1+x^2} dx$.

- 8 (a) Solve the differential equation $\frac{dy}{dx} = \frac{3y - 7x + 7}{3x - 7y - 3}$.

- (b) Solve $(D - 2)^2 y = 8(e^{2x} + \sin 2x + x^2)$.

OR

- 9 (a) Solve $\frac{dy}{dx} + \frac{y^2 + y + 1}{x^2 + x + 1} = 0$.

- (b) Solve $y'' - 2y' + 2y = x + e^x \cos x$.

- 10 (a) Show that the lines $2x + y - 3 = 0$, $3x + 2y - 2 = 0$ and $2x - 3y - 23 = 0$ are concurrent and find the point of concurrency.

- (b) Find the Laplace transform of $e^{2t} + 4t^3 - 2 \sin 3t + 3 \cos 3t$.

OR

- 11 (a) Find the coordinates of the vertex, focus, equation of directrix and axis of the following parabola $3x^2 - 9x + 5y - 2 = 0$.

- (b) Find the Laplace transform of $e^{2t} \cos^2 t$.

REMEDIAL MATHEMATICS

(For 2017 & 2018 admitted batches only)

Time: 3 hours

Max. Marks: 70

PART – A

(Compulsory Question)

1 Answer the following: (10 X 02 = 20 Marks)

- (a) Find the inverse of the matrix $A = \begin{bmatrix} 1 & 2 \\ 5 & 7 \end{bmatrix}$.
- (b) If $\tan A = 3/5$, find the values of $\sin 2A$ $\cos 2A$.
- (c) State Leibnitz's theorem.
- (d) Form the differential equation $y = ae^x + b$, where a, b are parameters.
- (e) Evaluate $\int x e^{2x} dx$.
- (f) Find $\frac{d}{dx}(5x^2 + 6 \sin x)$.
- (g) Find the value of $\lim_{x \rightarrow 0} \frac{\sin bx}{x \cos x}$.
- (h) Integrate $\int_0^{2\pi} \sin^2 x dx$.
- (i) Find the distance between the two parallel lines $3x + 4y + 3 = 0, 3x + 4y + 7 = 0$.
- (j) Find the value of $L\{\cos^2 2t\}$.

PART – B

(Answer all five units, 5 X 10 = 50 Marks)

- 2 (a) If $A = \begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}$ then show that $A(A - 3I)(A - 15I) = 0$.
- (b) In a triangle ABC, prove that $\cos^2 \frac{A}{2} + \cos^2 \frac{B}{2} - \cos^2 \frac{C}{2} = 2 \cos \frac{A}{2} \cos \frac{B}{2} \sin \frac{C}{2}$.

OR

- 3 From the top of the hill 200 meters high, the angle of depression of the top and bottom of a pillar on the level ground are 30° and 60° respectively. Find the height of the pillar.
- 4 (a) If $u = \tan^{-1} \left(\frac{x^3 + y^3}{x - y} \right)$, then prove that $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = \sin 2u$.
- (b) Find the n^{th} differential coefficient of $x^3 \log x$.

OR

- 5 (a) If $y = \tan^{-1} \left(\frac{\sqrt{1+x^2} + \sqrt{1-x^2}}{\sqrt{1+x^2} - \sqrt{1-x^2}} \right)$ for $0 < |x| < 1$, find $\frac{dy}{dx}$.
- (b) Find the derivative of $\log(x + \sqrt{x^2 - 1})$.

- 6 (a) Evaluate $\int \frac{dx}{(x+2)(x+3)}$.
- (b) Prove that $\int_0^{\pi/2} \frac{\sin^n x}{\sin^n x + \cos^n x} dx = \frac{\pi}{4}$.

OR

- 7 (a) Evaluate $\int_0^{2a} x^{7/2} (2a - x)^{-1/2} dx$.
- (b) Find the value of $\int_0^{\pi/2} \log(\tan x) dx$.

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- 8 (a) Solve the differential equation $\frac{dy}{dx} = \frac{y^2+1}{1+x^2}$.
(b) If $ax^2 + 2hxy + by^2 = 1$, prove that $\frac{d^2y}{dx^2} = \frac{h^2-ab}{(hx+by)^3}$.

OR

- 9 (a) Solve $y^1 + 2xy = e^{-x^2}$.
(b) Solve the differential equation $(1+x)y dx + (1+y)x dy = 0$.

- 10 (a) Find the area of the triangle formed by following straight lines and the coordinate axes:
(i) $2x - 4y - 7 = 0$.
(ii) $2x - 5y + 6 = 0$.
(b) Find the $L\{e^{-t} \cos ht + t^2\}$.

OR

- 11 (a) Find the locus of point P such that $PA+PB = 6$ where $A(0, 2)$ and $B(0, -2)$.
(b) Find the Laplace transform of $e^{-3t}(2 \cos 5t - 3 \sin 5t)$.

REMEDIAL MATHEMATICS

(For 2017 & 2018 admitted batches only)

Time: 3 hours

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PART – A

(Compulsory Question)

1 Answer the following: (10 X 02 = 20 Marks)

- (a) Find the determinant of a matrix $A = \begin{bmatrix} 1 & 3 & 3 \\ 1 & 4 & 3 \\ 1 & 3 & 4 \end{bmatrix}$.
- (b) Show that $\cos^2 48^\circ - \sin^2 12^\circ = \frac{\sqrt{5+1}}{8}$.
- (c) Find the derivative of the function $y = e^x + x^n + 5 \log x$.
- (d) Find the value of $\lim_{x \rightarrow a} \left(\frac{x \sin a - a \sin x}{x - a} \right)$.
- (e) Find the angle between the lines $2x + y + 4 = 0$ and $y - 3x = 7$.
- (f) Evaluate $\int \sqrt{x}(1-x) dx$.
- (g) Show that the points (2, 2), (6, 3), (4, 11) form a right angled triangle.
- (h) Solve the differential equation $\frac{d^2 y}{dx^2} - \frac{dy}{dx} = 0$.
- (i) Find the Laplace transform of $\sin 2t \sin 3t$.
- (j) Evaluate $\int \operatorname{cosec} x dx$.

PART – B

(Answer all five units, 5 X 10 = 50 Marks)

- 2 (a) Show that $\begin{vmatrix} a & b & c \\ a-b & b-c & c-a \\ b+c & c+a & a+b \end{vmatrix} = a^3 + b^3 + c^3 - 3abc$.
- (b) If $A+B+C=180^\circ$, prove that $\sin\left(\frac{A}{2}\right) + \cos\left(\frac{B-C}{2}\right) = 2 \cos\left(\frac{B}{2}\right) \cos\left(\frac{C}{2}\right)$

OR

- (a) Show that $\begin{vmatrix} 1 & a^2 & a^3 \\ 1 & b^2 & b^3 \\ 1 & c^2 & c^3 \end{vmatrix} = (a-b)(b-c)(c-a)(ab+bc+ca)$.
- (b) Find $\tan\left(\frac{\pi}{4} + A\right)$ and $\cot\left(\frac{\pi}{4} + A\right)$ in terms of $\tan A$ and $\cot A$.

- 4 (a) If $Y = x^4 \cos 3x$, find $1/n$ using Leibnitz's theorem.
- (b) Find the differential equation from the equation $y = Ax^3 + Bx^2$.

OR

- 5 (a) Solve $\frac{dy}{dx} = \frac{x-y}{x+y}$.
- (b) If $U = \log(x^3 + y^3 + z^3 - 3xyz)$, show that $\left(\frac{\partial}{\partial x} + \frac{\partial}{\partial y} + \frac{\partial}{\partial z}\right)^2 u = \frac{-9}{(x+y+z)^2}$.
- 6 (a) Evaluate $\int_a^b \sqrt{(x-a)(b-x)} dx$.
- (b) Evaluate $\int \frac{1}{4+5 \sin x} dx$.

OR

- 7 (a) Find the value of $\int_0^{\pi/4} \frac{e^{\tan x}}{\cos^2 x} dx$
- (b) Evaluate $\int x \cos^2 x dx$.

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- 8 (a) Solve $(x + 1) \frac{dy}{dx} + 1 = 2e^{-y}$.
(b) Solve $xy' + y + 4 = 0$

OR

- 9 (a) Obtain the differential equation of the coaxial circles of the system $x^2 + y^2 + 2ax + c^2 = 0$ where 'c' is constant.
(b) Solve the D.E. $(xy^2 + x)dx + (yx^2 + y)dy = 0$.

- 10 (a) Find the area of a triangle formed by the points (1, 2), (3, -4) and (-2, 0).
(b) Find the Laplace transform of $e^{-t} \cos 2t$.

OR

- 11 (a) Find the equation of locus of a point P, if A = (2, 3), B = (2, -3) and PA + PB = 8.
(b) Find $L\{e^{4t} \sin 2t \cos t\}$.

Code: 17T00106A

Pharm.D I Year Regular Examinations July/August 2018

REMEDIAL MATHEMATICS

(For 2017 admitted batches only)

Time: 3 hours

Max. Marks: 70

PART - A
(Compulsory Question)

1 Answer the following: (10 X 02 = 20 Marks)

- (a) In the matrix $A = \begin{bmatrix} 1 & 0 & -1 & -2 \\ 3 & 2 & 1 & 0 \\ 5 & 4 & 3 & 2 \end{bmatrix}$. Write the order of the matrix and write the elements $a_{13}, a_{21}, a_{33}, a_{24}, a_{23}$.
- (b) Evaluate $\begin{vmatrix} 3 & -1 \\ 0 & -5 \end{vmatrix}$.
- (c) Find $\frac{dy}{dx}$: $x = y + 2$.
- (d) Find $\frac{d^2y}{dx^2}$: $y = a^{mx}$.
- (e) Find $\int x^2 \left(1 - \frac{1}{x^2}\right) dx$.
- (f) Find $\int (x^{2/3} + 1) dx$.
- (g) What are differential equations? Write one example.
- (h) Find the order and degree of equation $\frac{d^2x}{dt^2} + w^2x = 0$.
- (i) Find the distance between the point (2,3), (1,5).
- (j) Find Laplace transformation of $\sin hat$.

PART - B

(Answer all five units, 5 X 10 = 50 Marks)

UNIT - I

2 Find x and y if $2x + 3y = \begin{bmatrix} 2 & 3 \\ 4 & 0 \end{bmatrix}$ & $3x + 2y = \begin{bmatrix} 2 & -2 \\ -1 & 5 \end{bmatrix}$.

OR

- 3 (a) If $x = a \cos \theta, y = b \sin \theta$, find the value of $\frac{x^2}{a^2} + \frac{y^2}{b^2}$.
- (b) If $\tan \theta = \frac{5}{12}$, find $\sin \theta \cos \theta \cot \theta$ and $\operatorname{cosec} \theta$.

UNIT - II

4 (a) If $x = (\cos \theta + \theta \sin \theta), y = (\sin \theta - \theta \cos \theta)$, show that $\frac{dy}{dx} = \tan \theta$.

(b) If $y = (x^2)^{\log x}$ find dy/dx .

OR

- 5 (a) If $u = e^{4x+3y}$ find $\frac{\partial u}{\partial x}, \frac{\partial u}{\partial y}$.
- (b) If $f(x) = \sin 6x \cdot \sin 3x$, find $f''(0)$.

UNIT - III

6 Find $\int \frac{1}{1+\tan x} dx$.

OR

7 Find $\int x \sin^{-1} x dx$.

UNIT - IV

8 Solve equation $\frac{dy}{dx} + xy = x$

OR

9 Solve using variable separable method $(1 - \cos y)dx + (1 - \cos x)dy = 0$.

UNIT - V

10 Find the equation of the straight line passing through the intersection of the lines $x+y+1 = 0$ and $2x-y+5 = 0$ and through the point (5,-2).

OR

11 Find the Laplace transform of

(i) $\left(\sqrt{t} - \frac{1}{\sqrt{t}}\right)^3$. (ii) $\cos t \cdot \cos 2t \cdot \cos 3t$.

Code: 14T00106A/ T0810006A

Pharm.D I Year Supplementary Examinations July/August 2018

REMEDIAL MATHEMATICS

(For 2016 and prior to 2016 admitted batches only)

Time: 3 hours

Max Marks: 70

Answer any FIVE questions
All questions carry equal marks

1 (a) Verify $(A + B)' = A' + B'$ for the matrices $A = \begin{bmatrix} -7 & -8 & 6 \\ 8 & 5 & 9 \\ 4 & 6 & 7 \end{bmatrix}$ and $B = \begin{bmatrix} 8 & 9 & 11 \\ 1 & 2 & 3 \\ 6 & 8 & 2 \end{bmatrix}$.

(b) Show that $\begin{bmatrix} -a^2 & ab & ac \\ ba & -b^2 & bc \\ ac & bc & -c^2 \end{bmatrix} = 4a^2b^2c^2$.

2 Prove that:

(a) $\frac{\tan\theta + \sec\theta - 1}{\tan\theta - \sec\theta + 1} = \frac{1 + \sin\theta}{\cos\theta}$.

(b) If $\theta + \phi = \frac{\pi}{4}$, then $(1 + \tan\theta)(1 + \tan\phi) = 2$.

3 (a) An equilateral triangle has one vertex at (3,4) and another at (-2,3). Find the coordinates of the third vertex.

(b) Find the derivatives of the locus of a point which is equidistant from the point (2,4) and the y-axis.

4 (a) If $z = t^5 - 3t^4 + 2t^3 + 8$, then find $\frac{dz}{dt}$. Also, find the value of the derivative at $t = 0, 1, 5$.

(b) Find the derivatives of the following functions with respect to x at the indicated points.

(i) $x + \sin x \cos x$ at $x = 0$ (ii) $\frac{1 - \sin x}{1 + \cos x}$ at $x = \frac{\pi}{2}$.

5 (a) Form the partial differential equation by eliminating the arbitrary constants $z = ax^3 + by^3$.

(b) Form the partial differential equation by eliminating the arbitrary function $z = yf(x^2 + z^2)$.

6 (a) Evaluate the following definite integrals: $\int_1^2 \frac{5x^2}{x^2 + 4x + 3} dx$.

(b) Evaluate the following definite integrals: $\int_0^1 x(1-x)^5 dx$.

7 (a) Solve the differential equation $e^{x-y} dx + e^{y-x} dy = 0$

(b) Solve $\frac{dy}{dx} + 2xy = e^{-x^2}$.

8 (a) Find the Laplace transform of $e^{2t} + 4t^3 - 2 \sin 3t + 3 \cos 3t$.

(b) Find $L(e^{-3t}(\cos 4t + 3 \sin 4t))$.

REMEDIAL MATHEMATICS

(For 2016 and prior to 2016 admitted batches only)

Time: 3 hours

Max Marks: 70

Answer any FIVE questions
All questions carry equal marks

- 1 (a) Find determination of $\begin{bmatrix} 2 & 4 & 3 \\ 1 & -4 & 1 \\ 0 & 3 & -7 \end{bmatrix}$.
- (b) Given the matrices A, B, C, $A = \begin{bmatrix} 2 & 3 & -1 \\ 3 & 0 & 2 \end{bmatrix}$, $B = \begin{bmatrix} 1 \\ 1 \\ 2 \end{bmatrix}$ $C = [1 \ 2]$ then find (AB)C.
- 2 (a) Prove that $\frac{\sec 8A - 1}{\sec 4A - 1} = \frac{\tan 8A}{\tan 2A}$.
- (b) Show that $4 \sin \frac{5\theta}{2} \cdot 4 \sin \frac{3\theta}{2} \cdot \cos 3\theta = \sin \theta - \sin 2\theta + \sin 4\theta + \sin 7\theta$
- 3 (a) Evaluate the limit:
$$\lim_{x \rightarrow 0} \frac{\sqrt{x^2 + 1} - \sqrt{-x^2 + 1}}{x}$$
- (b) Find $\frac{dy}{dx}$ when $y = 5x^2 + \sin x + 4e^x - \log x + \tan x$.
- 4 (a) If the acute angle between the lines $4x - y + 7 = 0$, $Kx - 5y - 9 = 0$ is 45° then find the value of K.
- (b) Find the derivative of the following function with respect to x, $e^x(x^5 + 3)$.
- 5 (a) Solve $\frac{dy}{dx} = (6x + y + 5)^2$.
- (b) Solve $\frac{dy}{dx} + 2\frac{dy}{dx} = e^x$.
- 6 Find the Laplace transform of:
- (a) $\frac{e^{at} - 1}{a}$.
- (b) $(t + 1)^3$.
- (c) $e^{-4t} \sin 2t \cos t$.
- 7 (a) Find the equation of the line passing through the point (3, -2) and perpendicular to the line $2x + 3y + 4 = 0$.
- (b) Find the angles of the triangle whose sides are $x + y - 4 = 0$, $2x + y - 6 = 0$ and $5x + 3y - 15 = 0$.
- 8 (a) If $A = \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix}$, show that $A^2 = 2A$ and $A^2 = 4A$.
- (b) If $A = \begin{bmatrix} 4 & 1 & 0 \\ 1 & -2 & 2 \end{bmatrix}$, $B = \begin{bmatrix} 2 & 0 & -1 \\ 3 & 1 & 4 \end{bmatrix}$, $C = \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix}$. Find the matrix X such that $(3B - 2A)C + 2X = 0$.

REMEDIAL MATHEMATICS

(For 2017, 2018, 2019, 2020 & 2021 admitted batches only)

Time: 3 hours

Max. Marks: 70

PART – A
(Compulsory Question)

1 Answer the following: (10 X 02 = 20 Marks)

- (a) Find the determinant of matrix $A = \begin{bmatrix} 4 & 2 \\ 3 & 2 \end{bmatrix}$. 2M
- (b) What is the use of Cramer's rule? 2M
- (c) Find the equation of the circle whose centre is (5, 7) and radius 4. 2M
- (d) Compute $\lim_{x \rightarrow 2} \frac{x}{x-1}$. 2M
- (e) If $\tan(A-B) = 7/24$ and $\tan A = 4/3$, then find A+B. 2M
- (f) Integrate $\int_0^{\pi/2} \cos^6 x \, dx$. 2M
- (g) Define: (i) Differential equation. (ii) Order of a differential equation. 2M
- (h) Solve: $\frac{dy}{dx} = \frac{x+y}{x}$. 2M
- (i) Find Laplace transform of e^{-4t} . 2M
- (j) Find the Laplace transform of t^2 . 2M

PART – B

(Answer all five units, 5 X 10 = 50 Marks)

- 2 (a) If $A = \begin{bmatrix} 1 & 2 \\ -1 & 3 \end{bmatrix}$ and $B = \begin{bmatrix} 2 & 1 \\ 1 & 1 \end{bmatrix}$. Find AB and BA. 5M

- (b) Show that $\begin{vmatrix} 1 & a & a^2 \\ 1 & b & b^2 \\ 1 & c & c^2 \end{vmatrix} = (b-c)(c-a)(a-b)$. 5M

OR

- 3 (a) Find $\lim_{x \rightarrow 3} 4x^2 - 1$. 5M

- (b) Prove that $\cot(A+15) - \tan(A-15) = \frac{4\cos 2A}{1+2\sin 2A}$. 5M

- 4 (a) Find the n^{th} derivative of $e^x (2x+3)^3$. 5M

- (b) Find the n^{th} derivative of $e^{2x} \cos^2 x \sin x$. 5M

OR

- 5 (a) If $u = \tan^{-1} \left(\frac{x^3 + y^3}{x+y} \right)$ prove that $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = \sin 2u$. 5M

- (b) If $x = r \cos \theta$, $y = r \sin \theta$, $z = z$ find $\frac{\partial(x, y, z)}{\partial(r, \theta, z)}$. 5M

Contd. in page 2

- 6 (a) Find the value of $\int x^2 \cos x \, dx$. 5M
(b) Find the value of $\int_0^1 \sqrt{x(1-x)} \, dx$. 5M
- OR
- 7 (a) Evaluate $\int x^2 e^x \, dx$. 5M
(b) Evaluate $\int_0^{\frac{\pi}{2}} \frac{\sin x \, dx}{(\sin x + \cos x)}$. 5M
- 8 (a) Solve $\frac{dy}{dx} = \frac{xy}{1+y}$. 5M
(b) Solve $y'' - 3y' + 2y = xe^{3x} + \sin 2x$. 5M
- OR
- 9 (a) Solve $\frac{d^2 y}{dx^2} - 7\frac{dy}{dx} + 12y = 0$. 5M
(b) Solve $\frac{d^2 y}{dx^2} - 5\frac{dy}{dx} + 6y = 4 \sin 4x$. 5M
- 10 (a) Find $L\{e^{-t} \sin 6t + t \cos 3t\}$. 5M
(b) Find the area of a triangle formed by the points (1, 2), (3, -4) and (-2, 0). 5M
- OR
- 11 (a) Find the Laplace transform of the function $\sin 5t \cos 2t$. 5M
(b) Find the Laplace transform of $t^2 e^{-3t} \sin 2t$. 5M

Code: 17T00106B

Pharm.D I Year Regular & Supplementary Examinations July/August 2019

REMEDIAL BIOLOGY

(For 2017 & 2018 admitted batches only)

Time: 3 hours

Max. Marks: 70

PART – A

(Compulsory Question)

- 1 Answer the following: (10 X 02 = 20 Marks)
- (a) What is the need of classification?
 - (b) Give the outline of modern system of classification of kingdom plantae.
 - (c) Define inflorescence and what are main types of inflorescence.
 - (d) Write about the classification of fruits.
 - (e) Name the common plants family Lilliaceae and write the diagnostic features of flower.
 - (f) Describe the structure and functions of bacterial cell wall.
 - (g) Write a short note on mitochondria of animal cell.
 - (h) What are the functions of connective tissue?
 - (i) Write a short note on Pisces.
 - (j) What are poisonous animals?

PART – B

(Answer all five units, 5 X 10 = 50 Marks)

- 2 Discuss about the leaf modifications with neat labeled diagrams.
- OR**
- 3 Explain in detail about the morphology of stem.
- 4 Describe the morphology of seeds with neat diagram.
- OR**
- 5 Discuss about the cymose inflorescence with help of neat diagrams.
- 6 Explain the taxonomic hierarchy of the family Umbelliferae.
- OR**
- 7 Explain the systemic hierarchy of two plants belongs to the family Rubiaceae.
- 8 Differentiate between plant cell & animal cell and describe the structure and functions of Golgi apparatus.
- OR**
- 9 Classify epithelial tissues and explain their structure & functions with the help of neat diagrams.
- 10 Explain the general characters of reptiles.
- OR**
- 11 Explain the important characters of Chelonia mydas.
